

## **Vibrations**

Some Preliminaries

#### Vibration = oscillation = anything that has a back-and-forth to it

Eg. Draw a pen back and forth over the same line, repeatedly:
When you come back to the same point defines one cycle, one vibration
If do it faster, your "frequency" is higher, your "period" is less.
But your "amplitude" (max. displacement) is the same – it's bigger if the line is bigger.

(We'll come back to these terms shortly)

#### Wave = vibration in both space and time

i.e. goes from one place to another: A vibration that propagates in space

# Vibration of a pendulum

• Suspend a stone at the end of a string and let it swing to and fro through small distances – makes a simple pendulum.

- Very regular oscillations if little friction eg found in some clocks.
- Period = time of a to-and-fro swing (i.e a cycle)
- For pendulum, period only depends on its length and g.

The longer the length, the longer the period, i.e. takes more time to come back. i.e. swings less frequently.

• Period does *not* depend on the mass. Quite analogous to the free-fall and inclined planes of Galileo – all masses fall at the same rate in vacuum; also all masses swing back and forth on end of a same-length string at the same rate.

• **DEMO** – swing various objects from a string and test not massdependent but is length-dependent.

• Also depends on the value of g eg the same pendulum oscillates slower on the moon than on earth

## **Clicker Question**

## **Wave Description**

- **Simple harmonic motion** describes pendulum as well as more general wave-like motion.
- E.g. a vertical spring with a mass at the end.

Hold pendulum bob with ink at the end over a conveyer belt, it traces out a **sine wave**: crests (high points)



troughs (low points)

So: **Amplitude = maximum displacement from equilibrium** (ie to crest or to trough) , and **Wavelength = crest-to-crest distance**, or, distance btn any successive identical parts

## Wave description cont.

Frequency = the number of to-and-fro vibrations in a given time (usually in a second).
 Unit of frequency
 One vibration per second = 1 Hertz (Hz) = 1 /s

Eg. Vibrating electrons are the source of radio waves

Electrons in this antenna vibrate 940 000 times per second – ie at 940 kHz. This is the freq of the radio waves produced.

AM radio waves are in kilohertz (kHz =1000Hz), while FM are in megahertz (MHz =  $10^{6}$  Hz).

Microwaves oscillate at gigahertz ( $GHz = 10^9 Hz$ )

• Period and frequency are just inverses of each other:

Period = 1/frequency

Frequency = 1/Period

Eg. If something makes four vibrations a second, its freq is 4 Hz. It takes  $\frac{1}{4}$  s to complete one vib, so its period is  $\frac{1}{4}$  s



## **Clicker Question**

### Wave motion

- Key point is that the **medium** (matter that wave is in) does *not* get propagated as the wave moves; rather, it is the *disturbance* that propagates
- Eg. **DEMO**: Consider a horizontal rope, with bright marker tied at one point. Shake it back and forth to generate a wave notice the disturbance propagates down rope, but the marker just moves back and forth. Finally, all points return to original position: The disturbance, not the medium, has travelled along.
- Eg. Water wave: drop stone in a pond. See expanding circles:

Water is not transported with the circles – rather, at any point, it moves up and down as wave passes by. (Can see this with a leaf on water's surface – it just bobs up and down) Again, the medium returns to where it started after wave has gone by.



• Via waves, <u>energy</u> can be transferred from a source to a receiver without the transfer of matter between the two points (eg light waves, sound waves, microwaves...)The larger the amplitude, the more the energy in the wave.

### Wave speed

Since speed = distance/time, can sit at a fixed point, measure distance between two crests (i.e. wavelength) and divide by how much time passes between arrival of subsequent crests (i.e. period):



- Holds for all types of periodic wave motion (water waves, sound, light...)
- Wave speed is a property of the type of wave and the medium, e.g. different water waves may have different wavelengths and periods but all have same wave speed in water.
- We often express this as  $v = f \lambda$

### Question

If a water wave oscillates up and down two times each second, and distance between crests is 3 m, what is its frequency, wavelength, and speed?

Frequency = 2 Hz, Wavelength = 3 m, Speed = 6 m/s

## **Clicker Question**

### **Clicker Question**

### **Transverse Waves**

When medium particles move at **right angles** to the direction of the disturbance.

Eg. Waves on a rope generated by shaking back and forth:

Can see this from watching the marker on the earlier demo. Or watching a leaf on the water's surface as a water wave passes – it goes up and down whereas wave is moving radially outward.



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Transverse waves include: water waves, waves on a stringed musical instrument, light, radio waves, microwaves...

## Longitudinal Waves

• When medium vibrates in the **same** direction as direction of wave travel.

- Wavelength-

-Wavelength

**Eg.** Slinky – when push and pull the end away and towards you:

 Medium vibrates parallel to direction of wave and energy flow. It's a compression wave – distance between compressed regions is wavelength (or distance between stretched regions)

#### called rarefaction

(Note that a slinky also can produce transverse waves. Shake end like:

• Longitudinal waves include: sound waves. Air molecs vibrate to and fro. Can also be thought of as a pressure wave.

## **Interference**

Property that distinguishes waves from particles: waves can **superpose** (= **overlap)**, and form an interference pattern, sometimes reinforcing each other, sometimes cancelling each other:

Eg. Water waves - created by two vibrating sources

When a crest of one wave meets a crest of another, they reinforce – "in phase".

When crest of one meets trough of other, they cancel out - "out of phase"



"grey" lines – out of phase

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Superposition principle: at every point, displacements add

## Standing waves

When forward and backward going waves interfere such that parts of the medium are always stationary.

**Eg.** Tie rope to a wall and shake. Wave going to wall gets completely reflected. Shake in such a way that set up a standing wave:



#### Standing wave DEMO:

Tie one end to wall, and shake at right frequency to get (a). Then shake twice as fast, and get (b). Three times as fast, get (c).



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• See also hands-on simulations at:

https://phet.colorado.edu/sims/wave-on-a-string/wave-on-a-string\_en.html

• Musical Instruments: work due to standing waves in string, or in air in a pipe in wind instrument. Can determine pitch from length of string, or length of air column...

## **Doppler Effect**

is when the frequency changes due to **motion** of the wave source or the receiver

Why?

Consider first stationary source (eg bug treading water with bobbing feet) : waves are circular because distance between crests (wavelength) is same in all directions.

Now consider if bug moves to the right at speed < wave speed. Centers of the circular waves move in direction of bug's motion.



Effect is that crests bunch at point B, spread out at point A. Since bug maintains same bobbing frequency, then point B sees waves coming more frequently i.e. *B observes higher frequency and shorter wavelength.* Similarly, *A observes lower frequency and longer wavelength.* 

# Doppler cont

• Nice animation of this at:

http://highered.mheducation.com/olcweb/cgi/pluginpop.cgi?it=swf::800::600::/sites/dl/free /0072482621/78778/Doppler\_Nav.swf::Doppler+Shift+Interactive

• Doppler effect is why a siren or horn of a car has a higher-than-normal pitch as it approaches you, and a lower-than-normal pitch as it leaves you:



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- Police speed radar operate on the Doppler effect! (see next chap for more)
- *Note:* don't confuse pitch(=frequency) with loudness(=amplitude)

• Also happens with light – where color is related to frequency, with high frequency being towards blue and low frequency is at the red end of spectrum

Hence, get "blue shift" of an approaching source (freq shifted up); and "red shift" of receding source (freq shifted down).

Eg. Distant galaxies show red shift

**Eg.** Spinning stars – can measure rate by comparing red shift of when it is turning away from us c.f. blue shift of when it turns towards us.





### **Question**

Is there a Doppler effect when the source of sound is stationary, and instead the listener is moving? If so, in what direction should listener move to hear a higher frequency?

Yes, there is a shift in frequency, because there is relative motion between the source and receiver. If you move toward a stationary sound source, you meet wave crests more frequently, so receive a higher frequency.

#### Bow waves

• When speed of source is as fast as wave speed, waves pile up: instead of moving ahead of source, they superpose on top right in front.

 Now, if source moves *faster* than wave speed, waves overlap at the edges as shown:
 Overlapping circles form a V

Called a **bow wave** eg can see when a boat speeds through water.



• Nice animations of these various Doppler phenomena at: http://en.wikipedia.org/wiki/Doppler\_effect



V becomes narrower as source speed increases.

## Shock Waves

- Essentially is a bow wave in 3-dimensions: the overlapping spheres form a cone.
- A supersonic aircraft moves faster than speed of sound so generates a shock sound wave.

An observer hears a **sonic boom** (sharp crack like sound) when the shell reaches him – from superposition of crests.



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Observer A and C hear nothing. Observer B is now hearing the sonic boom that C has already heard, and that A has not yet heard.

• Similarly, get a "water boom" from bow waves; eg a duck can be doused when the bow wave goes by.

#### Shock waves cont.

- Speed of sound ~ 340 m/s ~ 1245 km/h at sea-level
- We only hear a sonic boom with supersonic aircraft, *not* with subsonic – in the latter, sound waves continuously reach ear, no big overlap of crests.
- Only when craft moves faster than sound do the waves reach listener in one big burst.
- Note a common misconception is that sonic boom is heard just at the moment the craft reaches "sound barrier"- not true! It has likely been traveling supersonically for a while, with its shock wave passing other listeners (c.f. previous picture)
- Other examples of sonic booms: crack of a whip (tail of whip travelling faster than speed of sound), supersonic bullet...